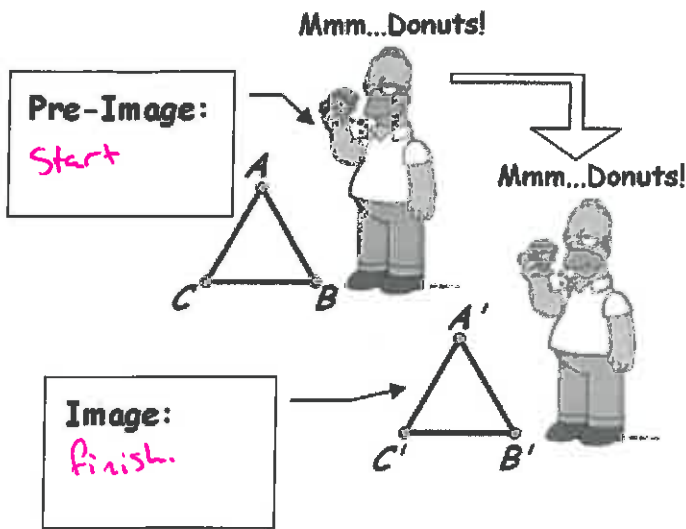
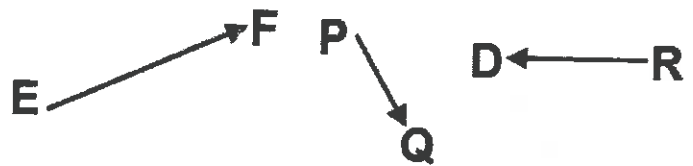


Rigid Motion – A *transformation* (movement) of a 2D figure in the plane such that **segment length** and **angle measure** are preserved.

Translation – Moving a 2D figure a given distance in a given direction. This is referred to as translating along a *Vector*.

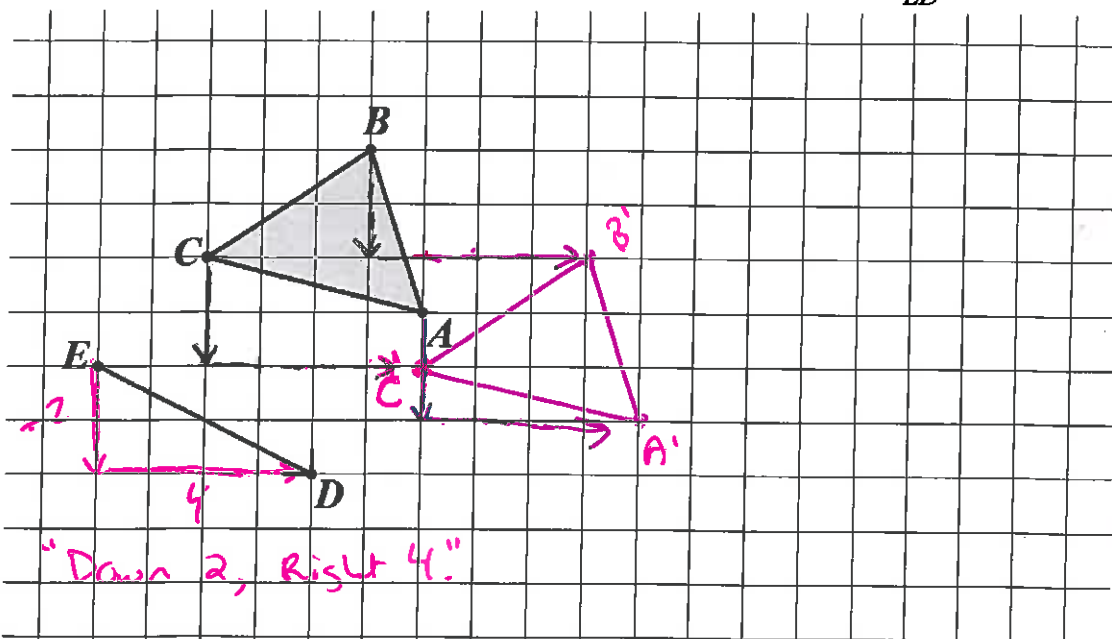


Vector – a distance and direction represented by a ray.

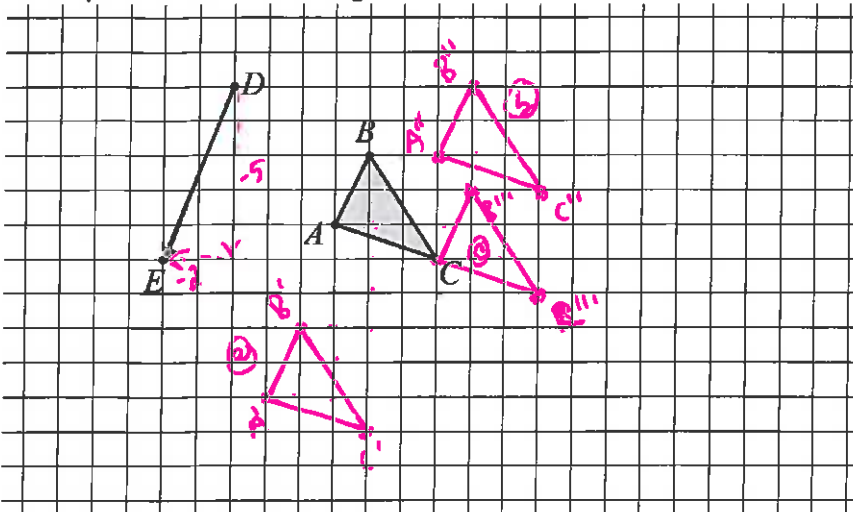


Each vector is identified by its direction + length.

1. Graph and label the image of $\triangle ABC$ under the transformation: $T_{\vec{ED}}$ ← translate along vector \vec{ED}



2. Graph and label the image of $\triangle ABC$ under each transformation:



a. Translate $\triangle ABC$ along vector \overline{DE} *Down 5, Left 2*

b. $T_{\langle 3, 2 \rangle}$ *Right 3, up 2*

c. $T_{\overline{AC}}$ *Right 3, down 1*

d. To be a Rigid Motion, translation must preserve **segment length** and **angle measure**. Given evidence from your graphs to demonstrate how each is preserved.

Segment Length

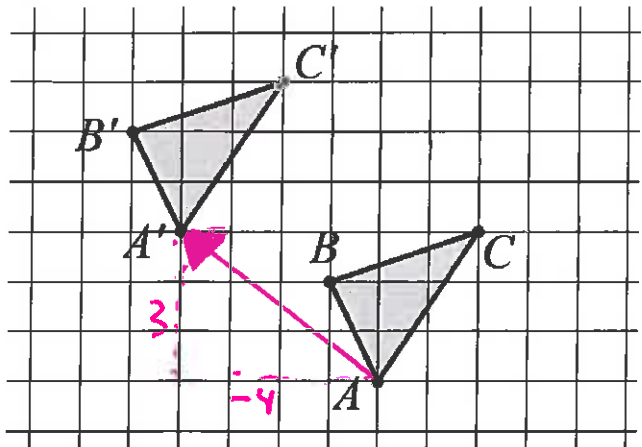
$$\left. \begin{aligned} AB &= \sqrt{1^2 + 2^2} = \sqrt{5} \\ A'B' &= \sqrt{1^2 + 2^2} = \sqrt{5} \end{aligned} \right\} \overline{AB} \cong \overline{A'B'}$$

Angle Measure

(a protractor or tracing paper may be helpful)

$$\angle A \cong \angle A' \text{ (measured with tracing paper)}$$

4.



a. Precisely describe the translation that maps $\triangle ABC$ onto $\triangle A'B'C'$.

Translate $\triangle ABC$ along vector $\langle -4, 3 \rangle$

or

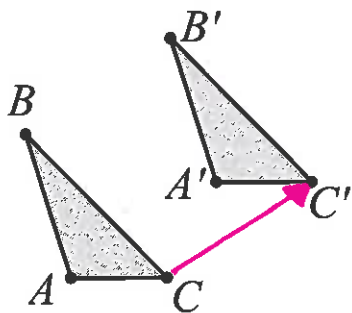
$$T_{\langle -4, 3 \rangle}$$

b. Precisely describe the translation that maps $\triangle ABC$ onto $\triangle A'B'C'$.

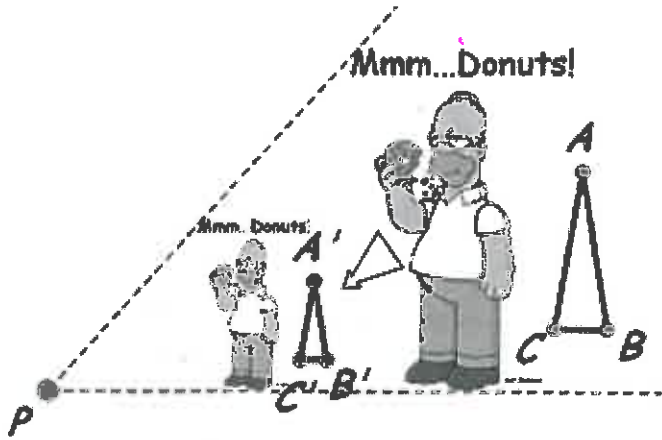
Translate $\triangle ABC$ along vector $\overrightarrow{CC'}$.

or

$$T_{\overrightarrow{CC'}}$$



Dilation – Enlarging or shrinking a 2D figure proportionally with respect to a given center point.



5. This picture of Homer Simpson and $\triangle ABC$ represents a Dilation.

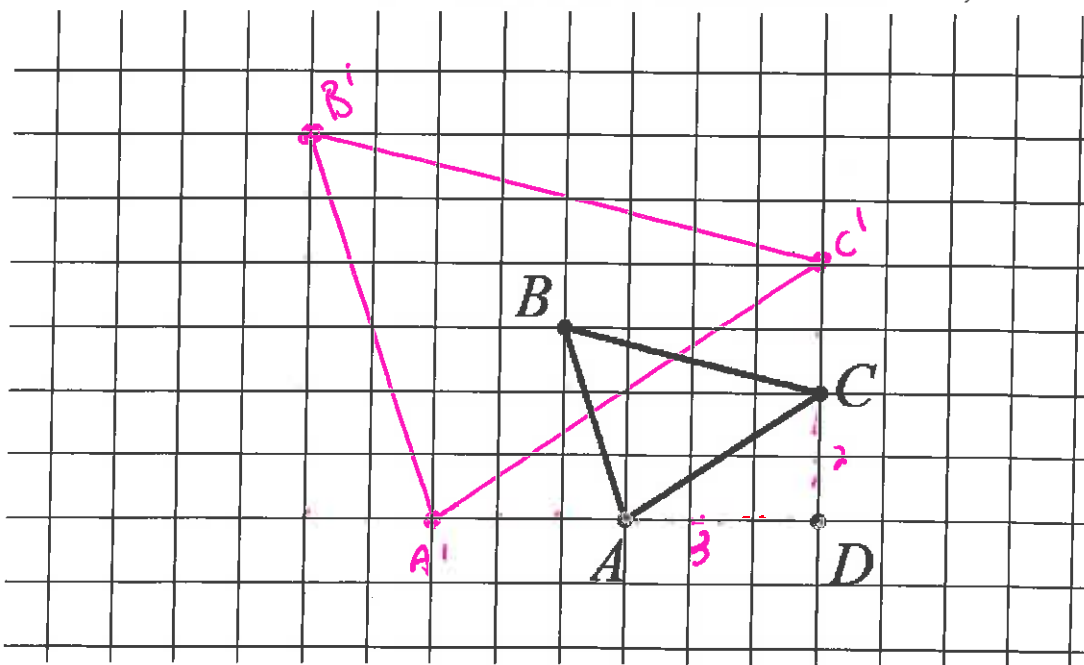
a. Which point is the center of dilation?

point P is the center.

b. Is Dilation a Rigid Motion? Explain why or why not.

It is not a rigid motion because segment length is not preserved.

6a. Graph and Label the image of $\triangle ABC$ under the transformation: $D_{D,2}$ Dilate around D by a factor of 2.



Double the distance from D to each point.

6b. To be a *Rigid Motion*, Dilation must preserve **segment length** and **angle measure**. Obviously segment length was not preserved. Give evidence from your graphs to demonstrate:

Segment Length Not Preserved

$$BA = \sqrt{1^2 + 3^2} = \sqrt{10}$$

$$B'A' = \sqrt{2^2 + 6^2} = \sqrt{40}$$

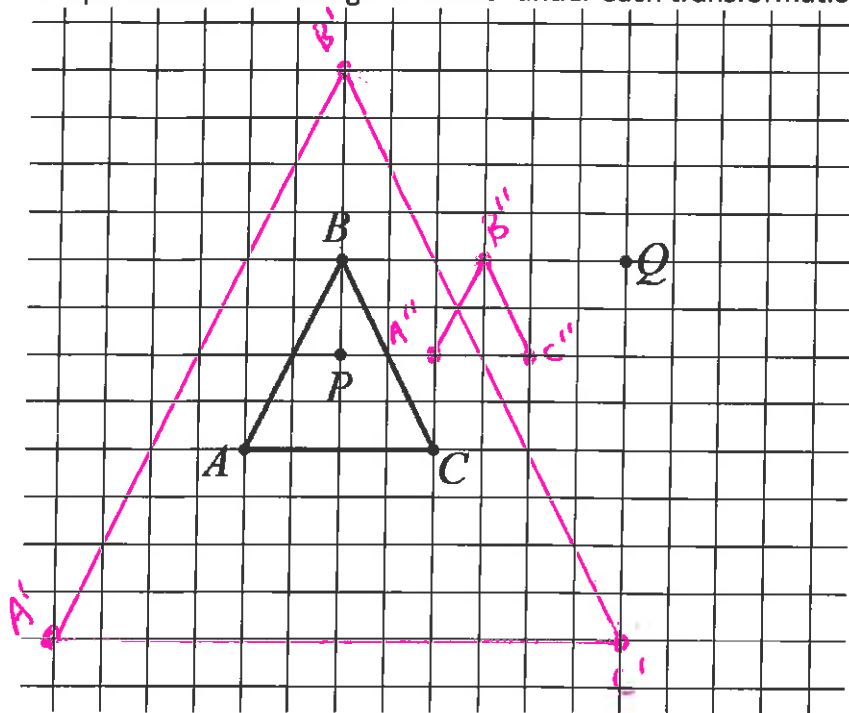
$$\overline{BA} \neq \overline{B'A'}$$

Angle Measure is Preserved

(a protractor or tracing paper may be helpful)

using tracing paper we can see $\angle A \cong \angle A'$.

7. Graph and label the image of $\triangle ABC$ under each transformation:



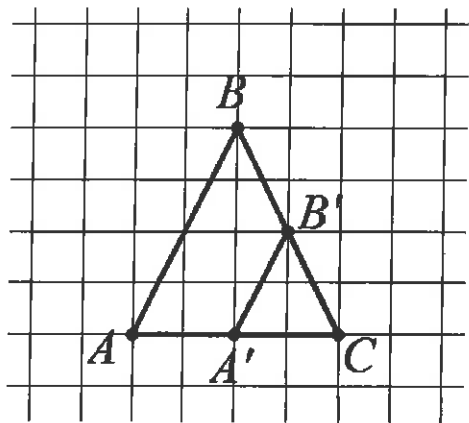
a. $D_{P,3}$

b. About center Q such that $\frac{A''B''}{AB} = \frac{1}{2}$

- want $A''B''$ to be half as long as AB .

- Dilate by factor of $\frac{1}{2}$.

8.



a. Describe precisely the transformation that maps $\triangle ABC$ onto $\triangle A'B'C'$.

$A'C'$ is half of AC . So...

Dilate $\triangle ABC$ by a factor of $\frac{1}{2}$ about C .

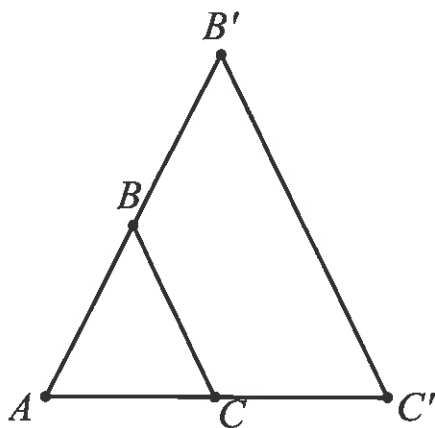
or

$D_{C, \frac{1}{2}}$

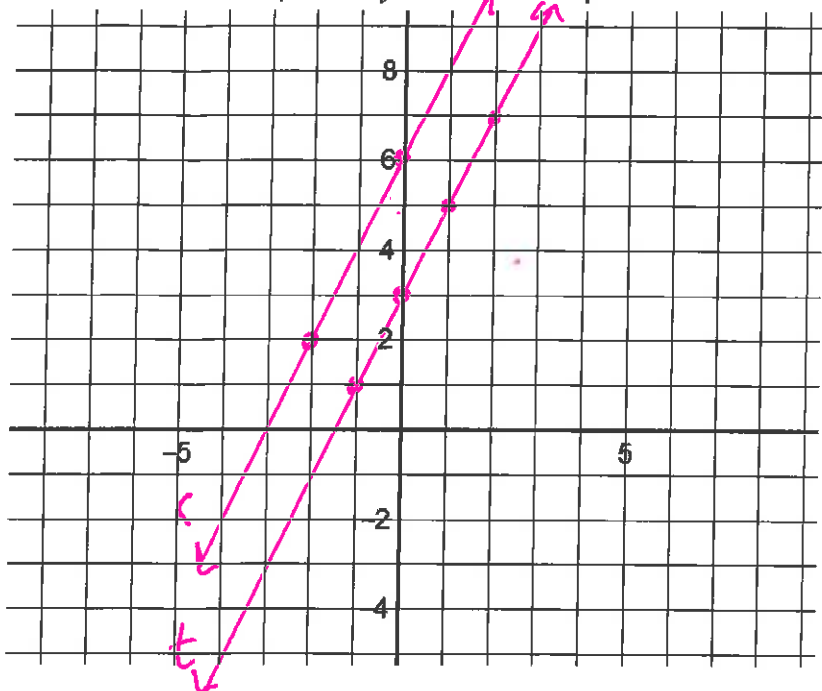
b. Describe precisely the transformation that maps $\triangle ABC$ onto $\triangle AB'C'$.

Dilate $\triangle ABC$ by a factor of $\frac{A'B'}{AB}$

About center A .



9a. Line t has the equation $y = 2x + 3$. Graph and label line t .



b. Line r is the image of line t under the transformation D_2 , using the origin as the center of dilation. Graph and label line r and write the equation that represents this line.

Slope = $\frac{2}{1}$
 y-int = 6

$y = 2x + 6$ is the equation of line r .

c. Compare the equations of the lines t and r . How do their slopes compare? How do their intercepts compare?

their slopes are =

the y-int of r is twice that of t .

d. The line $y = \frac{3}{2}x - 8$ is dilated by a factor of 4 with respect to the origin. Write the equation of the resulting line.

under D_4 slopes remain the same, but the y-int will be mult. by 4:

$y = \frac{3}{2}x - 32$

